

1. The above information shows that,
I. Mr. Jimoh's mother definitely has the ability for blood clotting.
II. Jimoh's mother was a carrier of the gene that predisposes one to excessive blood loss.
III. Mr. Jimoh's father had the gene that predisposes one to excessive blood loss.

Which of the above statements is/ are correct?
A. I only
B. II and III
C. III only
D. I and II

## Solution

Excessive blood loss (Haemophilia) is a sex-linked disorder which affects only males. Recessive genes that are carried on the X chromosome will produce the recessive phenotypes whenever they occur in males, since no dominant allele is present to mask them.

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## Answer: D

2. If Jimoh marries a normal woman that is not a carrier of the abnormal allele, what is the probability that they will give birth to a son that will produce excessive bleeding?
A. $3 / 4$
B. $1 / 2$
C. $1 / 4$
D. 0

## Solution

X X
$X^{c} \quad X^{c} X \quad X^{c} X$
Y XY XY
None of the sons will produce excessive bleeding.

## Answer: D

3. It is often possible to measure the amount of air normally present in the respiratory system and the rate at which ventilation occurs. The maximum amount of air that can be forcibly inhaled and exhaled from the lungs is called the vital capacity. The amount of air normally inhaled and exhaled with each breath is called the tidal volume. The residual volume is the air that always remains in the lungs, preventing the alveoli from collapsing. The expiratory reserve volume is the volume of air that can still be forcibly exhaled following a normal exhalation.

The total lung capacity will be equal to,
A. Tidal volume plus expiratory reserve volume
B. Vital capacity plus expiratory reserve volume
C. Vital capacity plus residual volume
D. Residual volume plus expiratory reserve volume.

## Solution

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Total lung capacity is the vital capacity, which is the maximum of air that can be inhaled or exhaled forcibly plus the residual volume, the air that always remains in the lungs preventing the alveoli from collapsing.

## Answer: C

4. Which of these is true of mountain dwellers in relation to people residing at sea level?
A. Mountain dwellers have greater vital capacity and enlarged thoracic cavity
B. Mountain dwellers have reduced vital capacity and compressed thoracic cavity
C. Mountain dwellers inhale a smaller amount of air than people living at sea level
D. Mountain dwellers havea reduced concentration of red blood cells than people living at sea level.

## Solution

Mountain dwellers would be expected to have the greater vital capacity. The partial pressure of $\mathrm{O}_{2}$ in the upper atmosphere is much lower than it is at sea level. So mountain dwellers generally have to inhale a greater volume of air than people living at sea level to extract the same amount of oxygen. Mountain dwellers generally have an enlarged thoracic cavity so that they can inhale and exhale a greater volume of air per breath.

## Answer: A

5. As an adaptive mechanism desert animals must conserve water by all means. The kidneys regulate the concentration of salt and water in the blood through the formation and excretion of urine. The kidney is composed of approximately one million units called nephrons. The kidneys of desert animals have modified nephrons which help them survive long periods without water. Which of these options best describes the expected modification?
A. A short collecting duct
B. A very long loop of Henle
C. A very short distal tubule
D. A large Bowman's capsule

## Solution

The loop of Henle concentrates sodium in the surrounding interstitial cells to establish a solute gradient for reabsorption of water. The longer the loop of Henle, the greater the distance the filtrate must travel through this gradient and with a greater distance; more water must be reabsorbed and conserved.
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## Answer: B

The amount of DNA present per cell at different stages during several nuclear divisions is represented inFigure 1. Use the diagram below (Figure 1) to answer questions 6-7

Figure1: Variations in DNA content of cell

## n

4n
2n
Amount of DNA per cell

## Z

W
X
Y

Time
6. What type of nuclear division is represented by Figure1?
A. Mitosis
B. Meiosis
C. Cytokinesis
D. None of the above.

## Solution

The figure represents reduction division $(2 n-n)$ i.e. meiosis.
Answer: B
7. What stages are represented by the red lines $\mathrm{W}, \mathrm{X}, \mathrm{Y}$ ?
A. Interphase, telophase I, telophase II.
B. Interphase, prophase, telophase II
C. Prophase, Interphase, telophaseI
D. Interphase, anaphase, telophase I

## Solution

Interphase - Replication of cell organelles; most of the DNA is replicated in Interphase.
Telophase I - Reduction of chromosome number occurs.
Telophase II - Nucleus now possesses half the number of single chromosomes of the original parent cell (haploid).

## Answer: A

8. The knowledge of the age structure of populations is important in the understanding of population dynamics because of the relevance of age to the reproductive role of organisms, including humans. A convenient way to picture age distribution in a population is to arrange the data in a form of polygon or age pyramid as shown below. Which pyramid in Figure 2 indicates a near stationary population?

## POST-REPRODUCTIVE

## (45 YEARS \& ABOVE

## REPRODUCTIVE

## (15-44 YEARS)

## PRE-REPRODUCTIVE

## (0-14 YEARS)

Fig 2: Age pyramid

A. X
B. Y
C. Z
D. None of the above

## Solution

There is a near balance between pre-reproductive, reproductive and post-reproductive age groups.

## Answer B

9. For any animal to survive in water, it must devise a means of obtaining oxygen for respiration. Fishes, for instance, obtain oxygen dissolved in water through their gills. Which of the following way(s) is (are) correct as sources of oxygen for aquatic insects?
i. Atmosphere
ii. Oxygen dissolved in water
iii. Air-containing cavities of submerged aquatic plants
A. iii;
B. i, ii;
C. i, ii,iii;
D. ii, iii.

## Answer C

10. Certain environmental conditions such as availability of water, optimum temperature and oxygen, must be present before the embryo of a seed will grow. Sometimes light is required for the seed to germinate. Seeds which require a stimulus of light for germination are usually relatively small. Which of following best explains the significance of this?
A. Small seeds commonly require light before germination will occur.
B. Small seeds commonly require light to inactivate the growth inhibitors in its coat before germination.
C. Small seeds have relatively small food reserves; it is therefore important that growing shoot reaches light quickly so that photosynthesis can start before the reserves are exhausted.
D. Small seeds commonly require light to find a suitable place for germination.

## Solution

Small seeds have relatively small food reserves; it is therefore important that growing shoot reaches light quickly so that photosynthesis can start before the reserves are exhausted.
Answer: C
11. Colloidal systems can be described in terms of the dispersed medium and dispersion medium as
a. Liquid - gas
b. Liquid - liquid
c. Liquid - solid
d. Solid-liquid

Examples of the systems (A) - (D) above include
I. Milk
II. Gelatin
III. Fog
IV. Paint

Which of the following is the correct match?
A. $\mathrm{a}-\mathrm{I}, \mathrm{b}-\mathrm{II}, \mathrm{c}-\mathrm{III}, \mathrm{d}-\mathrm{IV}$
B. $\mathrm{a}-\mathrm{II}, \mathrm{b}-\mathrm{I}, \mathrm{c}-\mathrm{IV}, \mathrm{d}-\mathrm{III}$
C. $\mathrm{a}-\mathrm{IV}, \mathrm{b}-\mathrm{III}, \mathrm{c}-\mathrm{II}, \mathrm{d}-\mathrm{I}$
D. $\mathrm{a}-\mathrm{III}, \mathrm{b}-\mathrm{I}, \mathrm{c}-\mathrm{II}, \mathrm{d}-\mathrm{IV}$

## Solution

An example of a liquid in gas colloidal system $=$ fog, liquid in liquid $=$ milk, liquid in solid $=$ gelatine, solid in liquid = paint

## Answer: D

12. Zinc of mass, 2.5 g containing zinc chloride as impurity was made to react with an excess of
dilute hydrochloric acid at $27^{\circ} \mathrm{C}$ and 760 mm Hg , liberating $780.0 \mathrm{~cm}^{3}$ of hydrogen. If the vapour pressure of water at $27^{\circ} \mathrm{C}$ is 14 mm Hg , what is the volume of $\mathrm{H}_{2}$ collected at STP? $\left(\mathrm{Zn}=65.0 ; \mathrm{H}=1.0 ; \mathrm{Cl}=35.5 ;\right.$ molar volume of gas at $\left.\mathrm{STP}=22.4 \mathrm{dm}^{3}\right)$
A. $\quad 746 \mathrm{~cm}^{3}$
B. $697 \mathrm{~cm}^{3}$
C. $\quad 750 \mathrm{~cm}^{3}$
D. $300 \mathrm{~cm}^{3}$

## Solution

$\mathrm{Zn}+2 \mathrm{HCl} \quad \mathrm{ZnCl}_{2}+\mathrm{H}_{2}$
therefore $=760-=746 \mathrm{mmHg}$
Let the volume of $\mathrm{H}_{2}$ at $\mathrm{STP}=\mathrm{V}_{2}$. Given that $\mathrm{P}_{1}=746 \mathrm{mmHg}, \mathrm{V}_{1}=780 \mathrm{~cm}^{3}, \mathrm{~T}_{1}=273+27=$ $300 \mathrm{~K}, \mathrm{P}_{2}=760 \mathrm{mmHg}, \mathrm{T}_{2}=273 \mathrm{~K}, \mathrm{~V}_{2}=$ ?

Using the expression, =

## Answer: B

13. A compound containing carbon $53.10 \%$, hydrogen $15.95 \%$ and nitrogen was found to have a molecular weight of $90 \mathrm{~g} / \mathrm{mol}(\mathrm{C}=12 \mathrm{~g} / \mathrm{mol} ; \mathrm{H}=1 \mathrm{~g} / \mathrm{mol} ; \mathrm{N}=14 \mathrm{~g} / \mathrm{mol})$. The molecular formula is
A. $\quad \mathrm{C}_{4} \mathrm{H}_{14} \mathrm{~N}_{2}$
B. $\quad \mathrm{C}_{2} \mathrm{H}_{7} \mathrm{~N}$
C. $\quad \mathrm{C}_{3} \mathrm{H}_{12} \mathrm{~N}_{2}$
D. $\quad \mathrm{C}_{2} \mathrm{H}_{14} \mathrm{~N}_{2}$

## Answer: A

Use Figure 3 to answer Question 14:
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## Battery <br> Switch <br> X

## Fruit

## Figure 3: Electric circuit

14. When the switch is closed, the bulb in the set up above will light if:
A. X is a section of an orange fruit
B. X is a section of dried avocado pear
C. X is a dish of distilled water
D. X is a beaker of $95 \%$ ethanol

## Solution

Orange fruit contains citric acid which ionises to produce $\mathrm{H}^{+}$, avocado pear is dry and so no ionisation can take place, distilled water does not contain ions.

## Answer A

15. For the oxidation-reduction reaction;

$$
\mathrm{K}_{2} \mathrm{Cr}_{2} \mathrm{O}_{7}+\mathrm{XH}_{2} \mathrm{SO}_{4}+\mathrm{YSO}_{2} \rightarrow \mathrm{~K}_{2} \mathrm{SO}_{4}+\mathrm{Cr}_{2}\left(\mathrm{SO}_{4}\right)_{3}+\mathrm{ZH}_{2} \mathrm{O}
$$

The values $\mathrm{X}, \mathrm{Y}$ and Z are:
A. 1,3,1
B. $4,1,4$
C. $3,2,3$
D. $2,1,2$

## Solution

From the reaction, $\mathrm{Cr}_{2} \mathrm{O}_{7}^{-}$is reduced to $\mathrm{Cr}^{3+}$ and $\mathrm{SO}_{2}$ is oxidized to $\mathrm{SO}_{4}{ }^{2-}$
$\mathrm{Cr}_{2} \mathrm{O}_{7}^{-}+14 \mathrm{H}^{+}+6 \mathrm{e}^{-} \rightarrow \mathrm{Cr}^{3+}+7 \mathrm{H}_{2} \mathrm{O}$ (Reduction) (i)
$3 \mathrm{SO}_{2}+6 \mathrm{H}_{2} \mathrm{O} \rightarrow 3 \mathrm{SO}_{4}{ }^{2-}+12 \mathrm{H}++6 \mathrm{e}^{-}$(Oxidation) (ii)
Addition of (i) and (ii) gives
$\mathrm{Cr}_{2} \mathrm{O}_{7}^{-}+2 \mathrm{H}^{+}+3 \mathrm{SO}_{2} \rightarrow 3 \mathrm{SO}_{4}^{2-}+2 \mathrm{Cr}^{3+}+\mathrm{H}_{2} \mathrm{O}$
$\mathrm{K}_{2} \mathrm{Cr}_{2} \mathrm{O}_{7}+\mathrm{H}_{2} \mathrm{SO}_{4}+3 \mathrm{SO}_{2} \rightarrow 3 \mathrm{~K}_{2} \mathrm{SO}_{4}+\mathrm{Cr}_{2}\left(\mathrm{SO}_{4}\right)_{3}+\mathrm{H}_{2} \mathrm{O}$
Hence $\mathrm{X}=1, \mathrm{Y}=3$ and $\mathrm{Z}=1$

Answer: A=1,3,1
16. Biochemists have discovered more than 400 mutant varieties of haemoglobin, the blood protein that carries oxygen throughout the body. A physician studying a variety associated with a fatal heart disease first finds its molar mass (M). She dissolves 21.5 mg of the protein in water at $5.0^{\circ} \mathrm{C}$ to make $1.50 \mathrm{~cm}^{3}$ of solution and measures an osmotic pressure of 0.00475 atm . What is the molar mass of this haemoglobin variety? $\left[\mathrm{R}=0.0821 \mathrm{l}-\mathrm{atm} \mathrm{mol}{ }^{-1} \mathrm{~K}^{-1}\right]$
A. $6.89 \times 10^{4} \mathrm{~g} \mathrm{~mol}^{-1}$
B. $6.79 \times 10^{4} \mathrm{~g} \mathrm{~mol}^{-1}$
C. $6.88 \times 10^{4} \mathrm{~g} \mathrm{~mol}^{-1}$
D. $6.87 \times 10^{4} \mathrm{~g} \mathrm{~mol}^{-1}$

## Solution

Combining unit conversion steps and solving for molarity:
$\pi=\mathrm{CRT}$
$\pi=0.00475 \mathrm{~atm} ; \mathrm{T}=273+5.0=278 \mathrm{~K} ; \mathrm{V}=0.00150 \mathrm{~L}$
$\mathrm{C}=\pi / \mathrm{RT}=0.00475 /\left(0.0821 \mathrm{latm} \mathrm{mol}{ }^{-1} \mathrm{~K}^{-1}\right)(278 \mathrm{~K})=2.08 \times 10^{-4} \mathrm{M}$
Finding the amount (mol) of solute:
Moles of solute $=\mathrm{Cx} \mathrm{V}=\left(2.08 \times 10^{-4} \mathrm{~mol} / l\right)(0.00150 l)=3.12 \times 10^{-7} \mathrm{~mol}$
Calculating molar mass of haemoglobin (after changing mg to g ):
$\mathrm{M}=0.0215 \mathrm{~g} 3.12 \times 10-7 \mathrm{~mol}=6.89 \times 104 \mathrm{~g} / \mathrm{mol}$

## Answer: A

17. The table below shows the pH ranges of some common indicators.

| Indicator | pH Range |
| :--- | :--- |
| Methyl Violet | $-0.3-1.8$ |
| Methyl Orange | $2.8-3.8$ |
| Congo Red | $2.8-4.8$ |
| Methyl Red | $3.8-6.1$ |
| Bromothylmol <br> Blue | $6.0-7.9$ |
| Phenol Red | $6.8-8.6$ |

Given that $\mathrm{k}_{\mathrm{a}}$ is $7.3 \times 10^{-10}$ for $\mathrm{KH}_{2} \mathrm{BO}_{3}$, choose an indicator that can be used for the titration of $0.1 \mathrm{M} \mathrm{KH}_{2} \mathrm{BO}_{3}$ with 0.10 M HCl ?
A. Methyl orange
B. Congo Red
C. Methyl Red
D. Phenol Red

## Solution

$\mathrm{KH}_{2} \mathrm{BO}_{3}+\mathrm{HCl} \rightarrow \mathrm{H}_{3} \mathrm{BO}_{3}+\mathrm{KCl}$
At equivalent point the concentration of $\mathrm{H}_{3} \mathrm{BO}_{3}$ produced $=0.050 \mathrm{M} . \mathrm{H}_{3} \mathrm{BO}_{3}$ then ionizes thus;
$\mathrm{H}_{3} \mathrm{BO}_{3}+\mathrm{H}_{2} \mathrm{O} \rightarrow \mathrm{H}_{3} \mathrm{BO}_{3}^{-}+\mathrm{H}_{3} \mathrm{O}^{+}$
$0.05 \mathrm{M} \quad x \quad x$
$\mathrm{k}_{\mathrm{a}}=\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{H}_{3} \mathrm{BO}_{3}^{-}\right] /\left[\mathrm{H}_{3} \mathrm{BO}_{3}\right]=\mathrm{x}^{2} / 0.05$
i.e., $7.3 \times 10^{-10}=x^{2} / 0.05$
$x=6.04 \times 10^{-6}$
$\mathrm{pH}=-\log \left(6.04 \times 10^{-6}\right)=5.22$
This pH is in the range of methyl red indicator which will be suitable for the titration

## Answer: C

18. A gas X at 1 atm is bubbled through a solution containing a mixture of $1 \mathrm{M} \mathrm{Y}^{-}$and $1 \mathrm{M} \mathrm{Z}^{-}$ at $25^{\circ} \mathrm{C}$. If the reduction potentials are in the order $\mathrm{Z}>\mathrm{Y}>\mathrm{X}$ then
A. $\quad \mathrm{Y}$ will oxidize X and not Z
B. $\quad \mathrm{Y}$ will oxidize Z and not X
C. $\quad \mathrm{Y}$ will oxidize both X and Z
D. $Y$ will reduce both $X$ and $Z$

## Solution

In redox reaction substances with:
(i) higher $\mathrm{E}^{0}$ values will oxidize those with lower $\mathrm{E}^{0}$ values
(ii) lower $\mathrm{E}^{\mathrm{o}}$ values will reduce those with higher $\mathrm{E}^{\mathrm{o}}$ values.

On the basis:
Y has higher $\mathrm{E}^{\circ}$ value than X ; Y will oxidize X
Y has lower $\mathrm{E}^{\circ}$ value than Z ; Y will not oxidize Z
$Y$ has lower $E^{\circ}$ value than $Z$; $Y$ will reduce $Z$
Y has higher $\mathrm{E}^{0}$ value than X ; Y will not reduce X
Answer: A
19. The air entering the lungs passes up in tiny sacs called alveoli, from which oxygen diffuses into the blood. The average radius of the alveoli is 0.0050 cm , and the air inside contains 14 mole percent oxygen. Assuming that the pressure in the alveoli is 1.0 atm and the temperature is $37^{\circ} \mathrm{C}$; calculate the number of oxygen molecules in one of the alveoli $\left(\mathrm{R}=0.08206 \mathrm{l}-\mathrm{atm} \mathrm{mol}^{-} \mathrm{K}^{-}\right)$
A. $\quad 1.7 \times 10^{11}$ oxygen molecules
B. $\quad 1.7 \times 10^{13}$ oxygen molecules
C. $\quad 1.7 \times 10^{12}$ oxygen molecules
D. $\quad 1.7 \times 10^{10}$ oxygen molecules

## Solution

Radius, $\mathrm{r}=0.0050 \mathrm{~cm}$
$\mathrm{T}=273+37=310 \mathrm{~K}$
The volume of one alveolus $=\mathrm{V}=(4 / 3) \pi \mathrm{r}^{3}$

$$
\begin{aligned}
& =(4 / 3) 3.12(0.0050 \mathrm{~cm})^{3} \\
& =5.2 \times 10^{-7} \mathrm{~cm}^{3}
\end{aligned}
$$

But $1 \mathrm{~L}=10^{3} \mathrm{~cm}^{3}$
Hence $V=5.2 \times 10^{-7} \times 10^{-3} \mathrm{~L}=5.2 \times 10^{-10} \mathrm{~L}$
No of moles, $n$ of air in one alveolus can be calculated from $P V=n R T$
$\mathrm{n}=\mathrm{PV} / \mathrm{RT}$
$=\left(1.0 \mathrm{~atm} \times 5.2 \times 10^{-10} \mathrm{~L}\right) /\left(0.08206 \mathrm{~L} \mathrm{~atm} \mathrm{~mol}^{-} \mathrm{K}^{-} \times 310 \mathrm{~K}\right)$
$=2.0 \times 10^{-11} \mathrm{~mol}$
1 mol of oxygen $=6.022 \times 10^{23}$ molecules
$2.0 \times 10^{-10}$ mol of oxygen $=2.0 \times 10^{-11} \times 6.022 \times 10^{23}$ molecules

$$
=12.044 \times 10^{12} \text { molecules }
$$

Air inside the alveolus is $14 \%$ oxygen,
Therefore no of oxygen molecules $=(14 / 100) \times 12.044 \times 10^{12}$
$=1.69 \times 10^{12}$ oxygen molecules

## Answer: C

20. Metabolism is the stepwise breakdown of the food we eat to provide energy for growth and function. A general overall equation for this complex process represents the degradation of glucose $\left(\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}\right)$ to $\mathrm{CO}_{2}$ and $\mathrm{H}_{2} \mathrm{O}$. This metabolic process involves many steps and its enthalpy $(\Delta \mathrm{H})$ is called the enthalpy of combustion. This is because the same quantity of heat is evolved whether we burn 1 mole of glucose in air or let the metabolic process break it down. Which of the following equations can be used to calculate the standard enthalpy of the metabolic process correctly?
(A) $\Delta \mathrm{H}^{0}=\left[\Delta_{\mathrm{f}} \mathrm{H}^{\circ}\left(\mathrm{CO}_{2}\right)+\Delta_{\mathrm{f}} \mathrm{H}^{\circ}\left(\mathrm{H}_{2} \mathrm{O}\right)\right]-\left[\Delta_{\mathrm{f}} \mathrm{H}^{\circ}\left(\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}\right)+\Delta_{\mathrm{f}} \mathrm{H}^{\circ}\left(\mathrm{O}_{2}\right)\right]$
(B) $\quad \Delta \mathrm{H}^{\circ}=\left[3 \Delta_{\mathrm{f}} \mathrm{H}^{\circ}\left(\mathrm{CO}_{2}\right)+3 \Delta_{\mathrm{f}} \mathrm{H}^{\circ}\left(\mathrm{H}_{2} \mathrm{O}\right)\right]-\left[\Delta_{\mathrm{f}} \mathrm{H}^{\circ}\left(\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}\right)+3 \Delta_{\mathrm{f}} \mathrm{H}^{\circ}\left(\mathrm{O}_{2}\right)\right]$
(C) $\quad \Delta \mathrm{H}^{\circ}=\left[3 \Delta_{\mathrm{f}} \mathrm{H}^{\circ}\left(\mathrm{CO}_{2}\right)+6 \Delta_{\mathrm{f}} \mathrm{H}^{\circ}\left(\mathrm{H}_{2} \mathrm{O}\right)\right]-\left[\Delta_{\mathrm{f}} \mathrm{H}^{\circ}\left(\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}\right)+3 \Delta_{\mathrm{f}} \mathrm{H}^{\circ}\left(\mathrm{O}_{2}\right)\right]$
(D) $\quad \Delta \mathrm{H}^{\circ}=\left[6 \Delta_{\mathrm{f}} \mathrm{H}^{\circ}\left(\mathrm{CO}_{2}\right)+6 \Delta_{\mathrm{f}} \mathrm{H}^{\circ}\left(\mathrm{H}_{2} \mathrm{O}\right)\right]-\left[\Delta_{\mathrm{f}} \mathrm{H}^{\circ}\left(\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}\right)+6 \Delta_{\mathrm{f}} \mathrm{H}^{\circ}\left(\mathrm{O}_{2}\right)\right]$

## Solution

$\Delta H^{\circ}=\left[6 \Delta_{f} H^{\circ}\left(\mathrm{CO}_{2}\right)+6 \Delta_{\mathrm{f}} \mathrm{H}^{\circ}\left(\mathrm{H}_{2} \mathrm{O}\right)\right]-\left[\Delta_{\mathrm{f}} \mathrm{H}^{\circ}\left(\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}\right)+6 \Delta_{\mathrm{f}} \mathrm{H}^{\circ}\left(\mathrm{O}_{2}\right)\right]$

## Answer: D

21. Given that the universal gravitational constant, $\mathrm{G}=6.7 \times 10^{-11} \mathrm{Nm}^{2} \mathrm{~kg}^{-2}$ and that the mass, M of the earth is $6.0 \times 10^{24} \mathrm{~kg}$, find the speed of a satellite that is fixed to permanently focus on the city of Abuja for broadcast of the 2010 IJSO competition.
A. $\quad 3.08 \times 10^{3} \mathrm{~ms}^{-1}$
B. $24 \mathrm{~ms}^{-1}$
C. $\quad 40 \mathrm{~ms}^{-1}$
D. $\quad 3.66 \times 10^{3} \mathrm{~ms}^{-1}$

## Solution

Centripetal force $=$ gravitational force $\Rightarrow, \mathrm{mv} 2 \mathrm{r}=\mathrm{GmMr}$, from where $\mathrm{v} 2=\mathrm{GMr}$ where $v$ is the velocity. Period, $T=2 \pi r v$ giving $r=T v 2 \pi$

Hence $v 3=2 \pi G M T \quad$ With $T=24 \mathrm{hr}=8.64 \times 10^{4} \mathrm{~s}$
$v=32 \pi \times 6.7 \times 10-11 \times 6.0 \times 10248.64 \times 104=3.08 \times 10^{3} \mathrm{~ms}$

## Answer: A

22. The surfaces of a biconvex lens have radii of curvature of 0.10 m and 0.15 m . If the refractive index of the glass is 1.5 , the power of the lens, correct to two significant figures, is
A. -8.3 D
B. -1.7 D
C. 1.7 D
D. 8.3 D

## Solution

Use

$$
\mathrm{n}=1.5 ; \mathrm{r}=0.10 \mathrm{~m} ; \mathrm{r}=0.15 \mathrm{~m}
$$

get $\quad f=0.12 \mathrm{~m}$
Power, $\mathrm{P}=$
Answer: D
23. Speed limit violators are usually monitored by the use of a radar gun which releases microwaves on the moving vehicle in short bursts. By applying the Doppler principle, the

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difference $(\Delta f)$ between the frequency of the microwave emitted by the radar gun and that reflected by the moving vehicle (and received by the gun) is obtained. The velocity (v) of the vehicle is then determined. If $\Delta \mathrm{f}$ is 2667 Hz and the frequency of the microwave is $1.0 \times 10^{10} \mathrm{~Hz}$, obtain the speed of the car.
A. $160 \mathrm{~ms}^{-1}$
B. $80 \mathrm{~ms}^{-1}$
C. $40 \mathrm{~ms}^{-1}$
D. $27 \mathrm{~ms}^{-1}$

## Solution

$\Delta \mathrm{f}=2 \mathrm{vfc}$ where c is the speed of light ;
Hence

$$
=3.0 \times 108 \times 26672 \times 1.0 \times 1010=40 \mathrm{~ms}
$$

## Answer: C

24. Solar radiation reaches the earth's atmosphere at a rate of $1353 \mathrm{Wm}^{-2}$. If $36 \%$ of this radiation is reflected back into space and $18 \%$ is absorbed by the earth's atmosphere, what maximum temperature would a black body on the earth's surface be expected to attain when left by itself? (Stefan-Boltzmann's constant $=5.67 \times 10^{-8} \mathrm{Wm}^{-2} \mathrm{~K}^{-4}$ ).
A. $\quad 120^{\circ} \mathrm{C}$
B. $\quad 63.9^{\circ} \mathrm{C}$
C. $\quad 50.7^{\circ} \mathrm{C}$
D. $\quad 31.4^{\circ} \mathrm{C}$

## Solution

Of the solar radiation reaching the earth's atmosphere
$36 \%$ is reflected back into space
$18 \%$ is absorbed by the earth's atmosphere
This implies that only $46 \%$ reaches the earth's surface
If absorbed by a black body, expect that the maximum temperature of this body is given by
where $I_{s c}=1353 \mathrm{Wm}^{-2}$

Answer: C

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25. A body of mass, $m$, resting on a smooth inclined plane at an angle $\theta$ to the horizontal is connected to a mass M over a smooth pulley (Fig. Q5). Find the velocity, v of the object of mass m when it has moved a distance b up the plane.
$\theta$
m
$m g s i n \theta$

## Smooth Pulley

M
A. $\quad v=2 g b M-m \sin \theta M+m$
B. $v=G b(M+m \sin \theta) M+m$
C. $\quad v=2 g b(m-m \sin \theta) M-m$
D. $\quad v=g b(M-m \sin \theta) M-m$

## Solution

Decrease in PE of system $=\mathrm{Mgb}-\mathrm{mgbsin} \theta$
Increase in $K E$ of system $=12(M+m) v 2$

## Answer: A

26. In using an axe to split firewood, the following energy forms are involved
i. Chemical (muscle) energy
ii. Mechanical potential energy of the axe;
iii. Chemical (binding) energy of wood, heat energy, sound energy and kinetic energy of wood fragments;
iv. Mechanical kinetic energy of the axe.

Which is the most likely sequence of the energy exchanges?
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A. (i), (ii), (iv), (iii)
B. (i), (iv), (iii), (ii)
C. (iv), (i), (ii), (iii)
D. (i), (ii), (iii), (iv)

## Answer: A

27. A jet of water travelling at a velocity of $20 \mathrm{~ms}^{-1}$ hits a wall normally. Calculate the pressure on the wall if the water does not bounce back. (Density of water $(\rho)=1.0 \times 10^{3} \mathrm{kgm}^{-3}$ ).
A. $\quad 8.0 \times 10^{5} \mathrm{~Pa}$
B. $\quad 4.0 \times 10^{5} \mathrm{~Pa}$
C. $\quad 2.0 \times 10^{5} \mathrm{~Pa}$
D. $\quad 2.0 \times 10^{-4} \mathrm{~Pa}$

## Answer: B

28. On a typical day during the World Cup tournament in South Africa, the air in a room is heated to $25^{\circ} \mathrm{C}$ while the outside air is $-2^{\circ} \mathrm{C}$. The area of the window of the room is $2 \mathrm{~m}^{2}$ and it is made of crown glass with thickness 2 mm and thermal conductivity $1.0 \mathrm{WK}^{-1} \mathrm{~m}^{-1}$. What is the power loss through the window?
A. $\quad 1.2 \mathrm{~kW}$
B. $\quad 2.7 \mathrm{~kW}$
C. $\quad 27 \mathrm{~kW}$
D. $\quad 50 \mathrm{~kW}$

## Solution

## Answer: C

29. The ratio of radii of two planets $P$ and $Q$ is $x$ and the ratio of their mean densities is $y$. Find the ratio of the acceleration of free fall on $P$ to that on $Q$ in terms of $x$ and $y$.
A. $x y$
B. $x 2 y$
C. $\mathrm{x}+\mathrm{y}$
D. $x y$
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## Solution

Density of any planet, $\rho=3 \mathrm{~g} 4 \pi \mathrm{Gr}$
$\rho p=3 g p 4 \pi G r p \quad ; \quad \rho Q=3 g Q 4 \pi G r Q$
$\rho p \rho Q=g p g Q r Q r p ; \quad g p g Q=\rho p \rho Q r p r Q=x y$
where $x=r p r Q$ and $y=\rho p \rho Q$
Answer: D
30. Two point charges, $q$ and $Q$, are separated as shown in the FQ10. Determine the electric potential difference between points X and Y .
$3 m$
4 m

## Y

$q=+3 n C$
$Q=-3 n C$
$\therefore$

X
$3 m$
A. 8.4 V
B. 7.2 V
C. 6.0 V
D. 0.0 V

## Solution

4m
3m
$3 m$
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## 5m

## $X$

## Y

$Q=-3 n C$
$q=-3 n C$

$$
\mathrm{rqX}=3 \mathrm{~m} \quad \mathrm{rqY}=5 \mathrm{~m}
$$

$$
\mathrm{rQX}=5 \mathrm{mrQY}=3 \mathrm{~m}
$$

; $\quad$ where $=9 \times 10^{9} \mathrm{mF}^{-1}$
$\mathrm{V}_{\mathrm{X}}-\mathrm{V}_{\mathrm{Y}}=7.2 \mathrm{~V}$

Answer: B

